

Therefore velocity $V = 10 \times \lambda = 10 \times 0.17 = 1.7 \text{ m/s}$ or 170 m/s 01 mark

Period T

Period, $T = \frac{1}{f} = \frac{1}{10} = 0.1 \text{ sec}$ 01 mark

(ii) Phase difference, $\theta = \frac{2\pi x}{\lambda}$

$= \frac{2 \times 3.14 \times 0.02}{0.17} = 0.74 \text{ rad/s}$ 01 mark

(c)(i) Doppler's principle and its application

- When the source approaches the listener or the listener approaches the source, or both approach each other, the apparent frequency is higher than the actual frequency of the sound produced by the source
- Similarly when the source moves away from the listener or when the listener moves away from the source, or when both move away from each other, the apparent frequency is lower than the actual frequency of the sound produced by the source
.....01 mark

Application of Doppler Effect

- Doppler shift in ultra-sound reflected from moving body tissues allows measurement of blood flow
- It is commonly used by obstetricians to detect foetal heart muscle pulsates
- Similarly, sonar makes use of the Doppler effect in determining the velocity of a submarine relative to a ship
- The electromagnetic waves, including light, are also subject to the Doppler Effect
- In air navigation, radar works by measuring the Doppler shift of high frequency radio waves reflected from moving aero-planes.
- The Doppler shift of star-light allows us to study stellar motion. When we examine light from stars in a spectrograph, we observe several spectral lines.

any one application01 mark

(ii) $v = \frac{c\Delta f}{2f\cos\theta}$ 01 mark

$v = \frac{1500 \times 3200}{2 \times 4000000 \cos 30}$

$V = 0.69 \text{ ms}^{-1}$ 01 mark

Volume rate of blood flow $= \frac{\pi d^2}{4} v = 1.4 \times 10^{-6} \text{ m}^3 \text{ s}^{-1}$ 01 mark

(d)(ii) The diameter of p^{th} and $(p+10)^{\text{th}}$ bright rings are given by

$D^2 = 4RL(p + \frac{1}{2})$

$D_{p+10}^2 = 4RL(p + 10 + \frac{1}{2})$ 01 mark

$D_{p+10}^2 - D_p^2 = 4RL(p + 10 + \frac{1}{2}) - 4RL(p + \frac{1}{2})$

$R = \frac{D_{p+10}^2 - D_p^2}{40\lambda}$

Substituting the given values it is clear that $R = 1.5 \text{ m}$ 01 mark

When the space between the glass and lens was filled with liquid with refractive index μ and λ is the wavelength of light in air while L_L is the wavelength of light in liquid

$$D_p^2 = 4RL_L \left(p + \frac{1}{2}\right) = \frac{4R}{\mu} \left(p + \frac{1}{2}\right)$$

$$D_{p+10}^2 = 4RL_L \left(p + 10 + \frac{1}{2}\right) = \frac{4R}{\mu} \left(p + 10 + \frac{1}{2}\right) \dots\dots\dots 01 \text{ mark}$$

$$D_{p+10}^2 - D_p^2 = \frac{40R \lambda}{\mu}$$

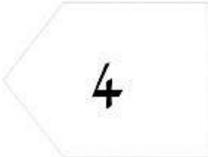
$$\mu = \frac{40R \lambda}{D_{p+10}^2 - D_p^2}$$

Substituting the given values it is clear that $\mu = 1.327 \dots\dots\dots 02 \text{ mark}$

3 (a)(i) Kinetic theory of gases states that “ all gases consists of molecules or atoms which are in continuous random motion” 02 mark

(ii) assumptions on deriving kinetic theory of gases

- The total volume of the molecules is negligible compared with the volume of the container
- The force of attraction between gas molecules is negligible
- The collision between gas molecules is elastic collision
- A sample of gases consist of a large number of identical molecules for statistical to be applied..... 02 mark @ 0.5 mark



(iii) Given the initial conditions, $P_1 = 15\text{atm}$, $V_1 = 30\text{litres}$, $T_1 = 27^\circ\text{C} = 273\text{K}$

After removing some oxygen Final conditions, $P_2 = 11\text{atm}$, $V_2 = V_1 = 30\text{litres}$, $T_2 = 17^\circ\text{C} = 290\text{K}$

From ideal gas equation $PV = nRT$, but $n = \frac{M}{M_R} \dots\dots\dots 01 \text{ mark}$

Then $PV = \frac{MRT}{M_R} \Rightarrow M = \frac{PVM_R}{RT} \dots\dots\dots 01 \text{ mark}$

Mass withdrawn $\Delta M = \frac{P_1 V_1 M_R}{RT_1} - \frac{P_2 V_2 M_R}{RT_2} \dots\dots\dots 01 \text{ mark}$

$\Delta M = \frac{\text{mass withdrawn}}{8.31 \times 300} - \frac{11 \times 101300 \times 0.03 \times 0.032}{8.31 \times 290} = 0.141\text{kg} = 141.0\text{g}$

Therefore mass of oxygen withdrawn = 141.0g..... 01 mark

(b)(i) Mean free path is the average distances a molecules travels between collisions. **WHILE**

Collision frequency is the number of collision made by molecules per second..... 02 mark

(ii) Given the diameter of argon, $d = 0.3 \text{ Angstrom} = 0.3 \times 10^{-10} \text{ m}$, number of moles, $n = 1 \text{ mole}$, pressure at S.T.P = 101300 N/m^2 temperature at S.T.P = 273 K , mean free path is given by

$$\lambda = \frac{KT}{\pi\sqrt{2}d^2P} \dots\dots\dots 01 \text{ mark}$$

$$\Rightarrow \frac{1.38 \times 10^{-23} \times 273}{\pi\sqrt{2}(0.3 \times 10^{-10})^2 (101300)} = 9.3 \times 10^{-6} \text{ m}$$

Therefore mean free path is $9.3 \times 10^{-6} \text{ m} \dots\dots\dots 01 \text{ mark}$

Collision frequency is given by $f = \frac{V}{\lambda}$ but $V = \sqrt{\frac{3RT}{M_R}} = \sqrt{\frac{3 \times 8.31 \times 273}{40 \times 10^{-3}}} = 412.6 \text{ m/s}$

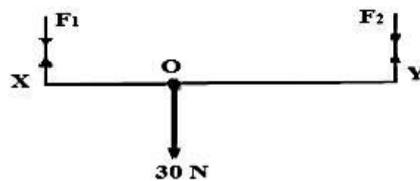
Then collision frequency $f = \frac{412.6}{9.3 \times 10^{-6}} = 4.44 \times 10^7 \text{ s}^{-1}$

...01 mark

(c)(i) tensile stress is the tensile force per unit perpendicular cross-sectional area,..... 01 mark

(ii)

Consider the fig. below



Extension is given by $e = \frac{FL}{AE} \dots\dots\dots 01 \text{ mark}$

Since the rod remain horizontally.

$e_x = e_y \dots\dots\dots 01 \text{ mark}$

$\frac{F_x L_x}{A_x Y_x} = \frac{F_y L_y}{A_y Y_y}$ but $L_x = L_y$ and $A_x = A_y \dots\dots\dots 01 \text{ mark}$

$\frac{F_x}{Y_x} = \frac{F_y}{Y_y} \dots\dots\dots (i)$

By principle of moment

Clockwise moment = anticlockwise moment.

$30 \times (OX) = F_y \times (OX + OY)$(ii).....01 mark

but $\frac{OY}{OX} = 2$

Then $F_y = 10\text{N}$ and $F_x = 20\text{N}$

Therefore from equation (i) we have $Y_y = \frac{F_y}{F_x} \times F_x = \frac{1.0 \times 10^{11} \times 10}{20} = 5 \times 10^{10} \text{ Pa}$

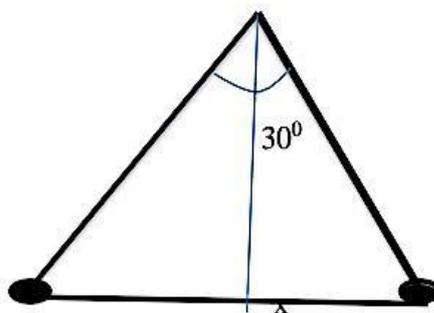
Young's modulus of a wire $y = 5 \times 10^{10} \text{ Pa}$ 02 mark

4. (a) (i) – it holds for stationary point charges only.....01 mark

- it does not give the direction of Coulomb's force.....01 mark

(ii), Referring to the figure , the coulomb force between the sphere in air is

$F = \frac{q^2}{4\pi\epsilon_0 r^2}$01 mark



in liquid

$F = \frac{q^2}{4\pi K\epsilon_0 r^2}$01 mark

Weight of sphere in air = mg

Apparent weight of sphere in liquid = $mg \left(1 - \frac{\rho}{\rho'}\right)$

Where ρ is density of material of sphere and ρ' is density of liquid

For equilibrium of vertical and horizontal forces , let T be tension in air and

T be tension in liquid

$T \sin\theta = F$ and $T \cos\theta = mg$

$T \sin\theta = F$ and $T \cos\theta = mg \left(1 - \frac{\rho}{\rho'}\right)$01 mark

Dividing each of four eqns

$$\tan\theta = \frac{F}{mg} = \frac{F}{mg(1-\rho)} \dots\dots\dots 01 \text{ mark}$$

$$\frac{F}{mg} = \frac{F}{mg(1-\rho)}$$

$$F = \frac{F}{(1-\rho)}$$

$$\frac{q^2}{4\pi\epsilon_0 r^2} = \frac{g^2}{(1-\rho)} \dots\dots\dots 01 \text{ mark}$$

$$1 = \frac{1}{K(1-\rho)}$$

$$K = \frac{1}{(1-\rho)}$$

$$K = \frac{1}{(1-0.8)}$$

$$K = \frac{1}{(1-0.5)} = 2 \dots\dots\dots 01 \text{ mark}$$

(b) (i) Potential energy of proton –electron system is; $U = \frac{q_1 q_2}{4 \epsilon_0 r} \dots\dots\dots 01 \text{ mark}$

$q_1 = 1.6 \times 10^{-19} \text{ C}$ $q_2 = -1.6 \times 10^{-19} \text{ C}$, $r = 0.53 \text{ \AA} = 0.53 \times 10^{-10} \text{ m}$. $\frac{1}{4 \epsilon_0} = 9 \times 10^9$

$$U = \frac{9 \times 10^9 (1.6 \times 10^{-19}) \times (1.6 \times 10^{-19})}{0.53 \times 10^{-10}} = -43.47 \times 10^{-19} \text{ J} = -27.2 \text{ eV} \dots\dots\dots 02 \text{ mark}$$

(ii) Kinetic energy = $\frac{1}{2}U = \frac{1}{2} \times 27.2 \text{ eV} = 13.6 \text{ eV} \dots\dots\dots 01 \text{ mark}$

Therefore, total energy $E = P.E + K.E = -27.2 \text{ eV} + 13.6 \text{ eV} = -13.6 \text{ eV} \dots\dots\dots 01 \text{ mark}$

The amount of energy to be done for the total removal of the electron is + 13.6eV

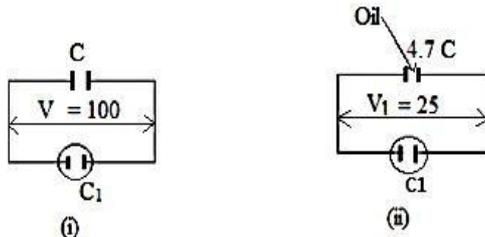
$\dots\dots\dots 01 \text{ mark}$

(c) Radius of the circular plates $r = 10 \text{ cm}$, distance between the plates $d = 2 \text{ mm}$,

Voltmeter readings $V = 100 \text{ V}$. $\epsilon_0 = 4.7$, second voltmeter reading $V_1 = 25$.

(i) Required to calculate the capacitance of the voltmeter.

Solution



Suppose V is the initial p.d across the air capacitor and voltmeter, and let C_1 be the voltmeter capacitor and C be the plates capacitance.

Then Total charge = $CV + C_1V = (C + C_1)V$ (i)01 mark

When the plates are filled with oil, the capacitance increases to $4.7 C$, and the p.d falls to V_1 but the total charge remains constant.

$$4.7CV_1 + C_1V_1 = (C + C_1)V$$

$(4.7 C + C_1) V_1 = (C + C_1)V$ (ii) 01 mark

$$\frac{4.7 C + C_1}{C + C_1} = \frac{V}{V_1} = \frac{100}{25} = 4$$

Therefore, $0.7C = 3C_1$, hence $C_1 = \frac{0.7 C}{3} = \frac{7}{30} C$

But $C = \frac{\epsilon_0}{Ad}$ where A is in m^2 and d is in metres

$$C = \frac{8.85 \times 10^{-12} \times (10 \times 10^{-2})^2}{2 \times 10^{-3}} F = 1.4 \times 10^{-10} F$$
 01 mark

Therefore, $C_1 = \frac{7}{30} \times 1.4 \times 10^{-10} F$ 01 mark

(ii) The assumptions made in arriving to the answer are

- The voltage recorded by the voltmeter is proportional to the scale reading
- Total charge is constant..... 01 mark
- P.d is the same for both capacitors01 mark

5.(a) (i)Magnetic force: Is a cross product of the velocity vector of the charged particle and the magnetic field vector (i.e $F = qv \times B$ 02 mark

Magnetic field strength

The S.I unit of magnetic field strength is Tesla T or $1kgA^{-1}s^{-2}$ 01 mark

(ii) Data given,

Magnetic field strength $B = 2.0 \times 10^{-5} T$

Current, $I = 1\text{A}$

Field due to current in a wire $= \frac{\mu_0 I}{2\pi r} = \frac{(4\pi \times 10^{-7}) \times (1.0\text{A})}{2\pi \times (0.01\text{m})} = 2.0 \times 10^{-5}\text{ T} \dots\dots\dots 02\text{ mark}$

Therefore, total field at A $= 2.0 \times 10^{-5}\text{ T} + 2.0 \times 10^{-5}\text{ T} = 4.0 \times 10^{-5}\text{ T} \dots\dots\dots 01\text{ mark}$

Total field at B $= 2.0 \times 10^{-5}\text{ T} - 2.0 \times 10^{-5}\text{ T} = 0.0 \dots\dots\dots 01\text{ mark}$

(b) (i) Lenz's law of electromagnetic induction states that; The magnitude and direction of the induced EMF is such that the current which it causes to flow (or would flow in a closed circuit) opposes the change which is producing it ($E = N \frac{d\phi}{dt}$).....02 mark

Or The magnitude of induced E.M.F is direct proportional to the rate of change of magnetic flux linking the coil

(ii) current, $I = 1.2\text{ mA}$, $R = 10\ \Omega$

Rate, $\frac{d\phi}{dt} = ?$

$E = N \frac{d\phi}{dt}$ but $E = IR = 1.2 \times 10^{-3} \times 10 = 1.2 \times 10^{-2}\text{ V}$, $N = 1 \dots\dots\dots 01\text{ mark}$

Therefore, $\frac{d\phi}{dt} = \frac{e}{N} = \frac{1.2 \times 10^{-2}}{1} = 1.2 \times 10^{-2}\text{ Wb/sec} \dots\dots\dots 03\text{ mark}$

(c) Given magnetic induction, $B = 1.2\text{ Tesla}$, radius of a circle, $R = 49\text{ cm} = 0.49\text{m}$

(i) Speed of the particle $V = ?$

(ii) Kinetic energy of the particle = ?

(i) From $Bev = \frac{mv^2}{r}$, therefore, $v = \frac{Ber}{m} \dots\dots\dots 01\text{ mark}$

$V = \frac{1.2 \times 1.6 \times 10^{-19} \times 0.49}{9.1 \times 10^{-31}\text{ kg}} = \frac{9.408 \times 10^{-19}}{9.1 \times 10^{-31}}$

$V = 1.03 \times 10^{12}\text{ m/s} \dots\dots\dots 02\text{ mark}$

Kinetic energy $= \frac{1}{2}mv^2 \dots\dots\dots 02\text{ mark}$

(d) (i) Curie's temperature is the temperature at which ferromagnetic material changes to paramagnetic 01 mark

(i) Hysteresis is the lagging of magnetic flux density behind the magnetizing force 01 mark

6(a)(i) No, it is not necessary that if energy supplied to an electron is more than work function, the electron will come out. The electron after receiving energy may lose energy to the metal due to collisions with atoms of metal. Therefore most of electrons get scattered into the metal. Only few electrons in the metal may come out of metal surface for whom the incident energy is greater than work function of metal02 mark

(ii) - on reducing the distance the intensity increases. Photoelectric current increases with increase in distance01.5 mark

- stopping potential is independent of intensity and therefore remains unchanged01.5 mark

(b) (i) Why are the energies of various energy levels of hydrogen are negative.

The reason is that, an atom of hydrogen consists of proton its nucleus and an electron around it. The two particles are held together by the columbic force of attraction. When the electrons and the nucleus are at the infinite distance apart, they do not interact with each other. The energy of the electron and the nucleus when are separated from each other by infinite distance is arbitrary taken as zero. When the two particle are brought close to each other, the attraction interaction starts developing. Due to this interaction a certain amount of energy is released. Thus the energy of the system fall below zero (i.e. energy becomes negative)

OR

Negative energy shows that an electron is bound to atom..... 01 mark

(ii) Total energy of electron in Hydrogen atom is;

$$E = -13.6\text{eV} = -13.6 \times 1.6 \times 10^{-19} \text{ J} = -2.2 \times 10^{-18} \text{ J}.....01 \text{ mark}$$

$$\text{But, } E = \frac{e^2}{8\pi\epsilon_0 r}.....01 \text{ mark}$$

$$\text{Therefore, } r = \frac{e^2}{2(4\pi\epsilon_0)E} = \frac{-9 \times 10^9 \times (1.6 \times 10^{-19})^2}{2 \times (-2.2 \times 10^{-18})} = 5.3 \times 10^{-11} \text{ m}.....01 \text{ mark}$$

$$\text{Velocity, } v = \frac{e}{\sqrt{4\pi\epsilon_0 m r}}, \text{ where, } m = 9.1 \times 10^{-31} \text{ kg}$$

$$V = \frac{1.6 \times 10^{-19}}{\sqrt{\frac{9.1 \times 10^{-31} \times 5.3 \times 10^{-11}}{9 \times 10^9}}} = 2.2 \times 10^6 \text{ m/s}.....02 \text{ mark}$$

(c) (i) **Binding energy of atom:**

- Is the energy required to break up the nucleus into its components of protons and neutron01 mark

Mass defect of atom: is the difference between mass of the nucleons and electrons of an atom with the mass of the atom01 mark

(ii) Binding energy of the Helium atom which consist of 2 proton and 2 neutrons and 2 electrons.

Mass of Helium atom = 4.002600 u, Mass of proton, $m_p = 1.00728$ u, mass of neutrons = 1.00867u mass of electron, $m_e = 0.00055$ u

$$1u = 932eV$$

The total mass of the particle is $M_t = 2(M_p) + 2(M_n) + 2(M_e)$

$$= 9(1.00728) + 2(1.00867) + 2(0.00055) = 4.003300u.....01 mark$$

The mass defect = Mass of nucleon – mass of nucleus

$$= 4.003300 - 4.002600 = 0.00304 u 01 mark$$

$$\text{Binding energy} = 932 \times \text{mass defect} = 932 \times 0.00304 u = 28.3 \text{ MeV} 01 mark$$

(d) Calculate the energy released when 10 kg of ${}^{235}_{36}U + {}^1_0n \rightarrow {}^{141}_{56}Ba + {}^{92}_{36}Kr + 3{}^1_0n$

Mass of ${}^{235}_{36}U = 235.04u$, Mass of ${}^{141}_{56}Ba = 140.91u$, mass of ${}^{92}_{36}Kr = 91.91u$, mass of

$${}^1_0n = 1.01u, 1u = 932 \text{ MeV and } N_A = 6.0 \times 10^{23} \text{ mol}^{-1}$$

$$\text{Mass difference} = (235.04 + 1.01) - (140.91 + 91.91 + 3 \times 1.01) = 0.20 u$$

$$\text{Energy released} = 0.2 \times 932 = 186.4 \text{ MeV} 01 mark$$

$$235.04 \times 10^{-3} \text{Kg of } {}^{235}_{36}U \text{ contains } 6.02 \times 10^{23} \text{ atoms}..... 01 mark$$

$$10 \text{ kg of } {}^{235}_{36}U \text{ contains } \frac{10 \times 6.02 \times 10^{23}}{235.04 \times 10^{-3}} = 2.56 \times 10^{25} \text{ atoms} 01 mark$$

$$\text{Energy released by 10 kg of } {}^{235}_{36}U = 2.56 \times 10^{25} \times 186.4 = 4.77 \times 10^{27} \text{ MeV}$$

.....01 mark